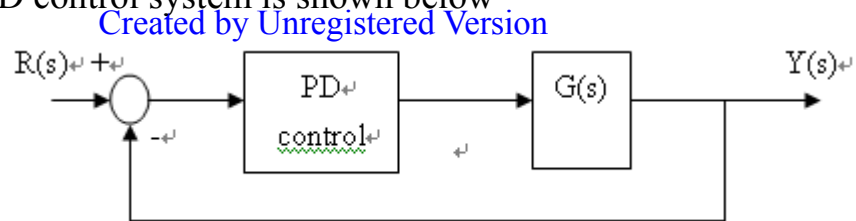


自動控制  
UNREGISTERED

1. The block diagram of a PD control system is shown below



where  $G(s) = \frac{2}{s^2 + 1}$  and the transfer function of the PD controller is  $G_c = K_p + K_D s$

(a) Find  $K_p$  and  $K_D$  on which the damping is critical and the natural undamped frequency  $\omega_n$  is 5 rad/sec.

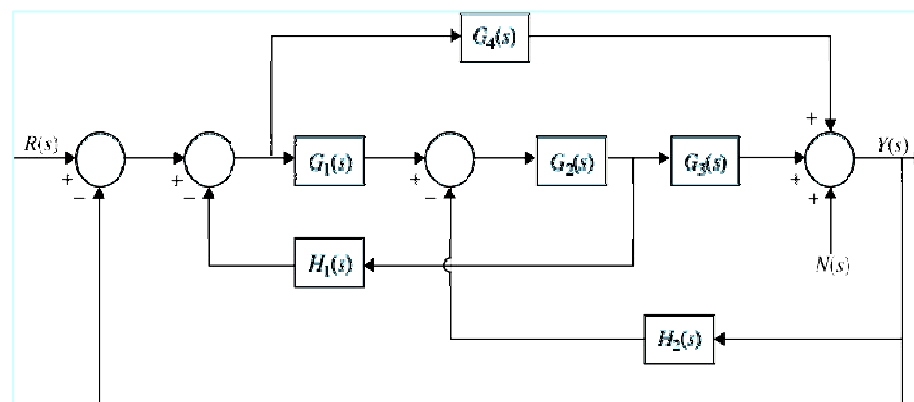
(b) From part (a), with unity-step input, find the steady-state error.

(c) From part (a), with unity-step input, find the steady-state value of  $y(t)$ .

(d) Find the parabolic-error constant  $K_a$ .

(20 points)

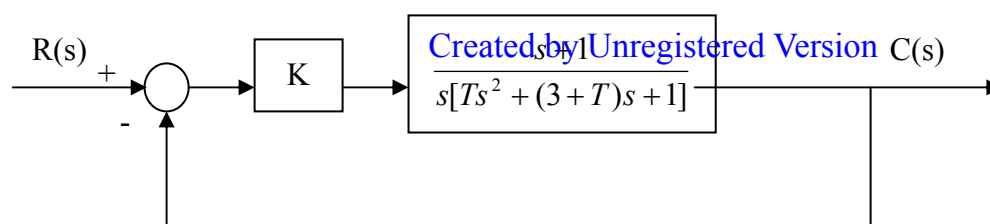
2. For a system block diagram shown below



Please find the transfer function  $\frac{Y(s)}{R(s)} = ?$

(15 points)

3. Please find the range of  $K$  and  $T$  for the stability of the closed-loop system ?



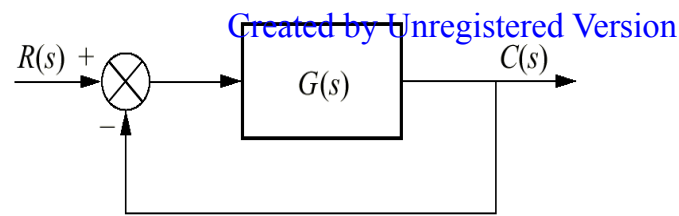
(15 points)

4. Consider a unity feedback system with open-loop delay transfer function as shown in the following

figure, where  $G(s) = \frac{3e^{-sT}}{s(s + 2\sqrt{2})}$ . What is the maximum time delay  $T$  without destroying the

closed-loop stability?

自動控制  
UNREGISTERED



(15points)

5. A control system is represented by the following state equations:

$$\dot{x}_1 = 3x_1 - 8x_2$$

$$\dot{x}_2 = 4x_1 + u$$

The control law is designed as the following state feedback form

UNREGISTERED

$$u = -ax_1 - bx_2$$

where a and b are real constants. Determine and sketch the region of a and b for the overall system to be stable. Please put a as the x-axis and b as the y-axis.

(20 points)

6. For a dynamic system with state equations:

$$\dot{x}_1 = -x_2 + u$$

$$\dot{x}_2 = -3x_1 + 2x_2 - 3u$$

$$y = x_1$$

(a) Determine the controllability and observability of the system.

(b) Find the transfer function  $\frac{Y(s)}{U(s)}$

(c) Is it possible to use output feedback control  $u = -ky$  for arbitrary pole assignment?

(15 points)

UNREGISTERED

Created by Unregistered Version